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Abstract. Accurate iris movement detection and tracking is an important and widely used step in many Human-computer interactive applications. Among the eye features, eye corners are considered as stable and reliable reference points to measure the relative iris motion. In real time scenarios, the presence of spectacles prohibit the current state-of-the-art methods to yield accurate detection as the appearance of eye corners changes considerably due to the glare and occlusion caused by them. We term this problem as the Spectacle problem. In this paper we review the available single and multiple image based spectacle problem removal techniques and highlight the pros and cons of the approaches. For this state-of-the-art report, we investigated research papers, patents and thesis presenting the basic definitions, terminologies and new directions for future researches.

Keywords: Eye corners \cdot detection \cdot spectacle problem \cdot specular reflection \cdot glare \cdot occlusion.

1 Introduction

Eyes are one of the most important human facial features. They provide information about a person's identity, intentions and attention levels [44]. Detection, localization, and recognition of eye features is an important step in face detection, Biometric, Human-computer interaction (HCI) and many other diverse applications. Of all the applications, iris movement estimation is a very challenging task as it involves in continuous tracking of eye features. Many algorithms employ projective geometric parameters like the distance between the camera and the subject to estimate the eye position coordinates. However, these measurements will be erroneous when the subject is free to move his/her head. Hence, a relative measurement of pupil position with respect to other fixed reference point(s) may be appropriate to alleviate the problem [4]. Among the eye features, eye corners have the advantage of being robust to various facial expressions, gaze direction and eye status [4,7,10,21,43,44,54,56]. Because of these advantages, localization of eye corners is of great importance as they offer robust reference points.

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1.1 Eye corner detection

Compared to a large amount of iris detection methods, methods related to eye corner detection are limited [4, 49, 54]. One of the prime reason being lack of proper semantic definition of eye corners. Generally, eye corners near to the nose are called the inner eye corners, and the eye corners towards the ears are called the outer eye corners. In literature there are three semantic definitions of eye corners: (a) The intersection between the upper and lower eyelids [1, 7, 10, 13, 16, 41, 49, 54–56]; (b) Eye corner is classified as a pit under image topography perspective [4]; (c) The end of the sclera is labeled as the eye corner [34, 43]. Based on these definitions, various eye corner detection algorithms are available in the literature, which can be broadly classified into three categories namely: Shape based, Feature based, and Sample based models.

Shape based eye corner detections Shape-based models [16,21,34,43,54,59] explores the geometrical shape details between eyes and other facial features in the human face context. Some algorithms assume an eye template consisting of simple geometric primitives and energy function for feature detection. Though shape based model detects eye corners reliably, they suffer from the following lacunas:

- The efficacy of the detection is mainly influenced by the formulation of the template.
- As the template is predetermined, it may not be able to handle real-time scenarios like head pose change.
- The execution time depends on how close the template is initiated to the eye corners. Therefore these approaches may not yield real-time results.

Feature based eye corner detections Feature based methods explore pertinent eye properties like local structure and image intensities to identify the eye corners [35]. No pre-determination and pre-processing of templates is required in these methods. These methods are easy to implement and can be used in real-time operations. In literature, there are two types of feature based corner detection schemes: edge-based and corner detection based. Generally, the edge-based corner detection methods like [52, 56] are more reliable than the corner-based methods [4, 62]. The main challenge for general purpose corner detectors is the fact that image characteristics of eye corners can largely vary between subjects [48, 49]. As a result, reliable detection might be possible only under good imaging conditions.

Sample based eye corner detections Sample based eye corner detection methods [8, 19, 49, 60] try to extract useful visual features from photometric appearance, based on which eye model is learnt from a large set of training images. With the advent of appearance based approaches, many traditional approaches have been replaced by deep-learning methods like Convolutional Neural Networks (CNN). The major advantage of CNN based approaches is it's precision

while the limitation is that the efficiency of the methods totally depends on the representative variability of eye appearance in the training data. Due to the usage of large-datasets for training—which involves high performance computing analysis—the brevity and ease of administration is quite questionable.

1.2 Summary

No matter what the approach is, accurate detection and localization of eye features in an unconstrained environment is an ever challenging task due to the high degree of eye's appearance variability. This variability is caused either by intrinsic dynamic features of the eyes or by external factors like spectacles, hair and ambient environment changes. An extensive literature review on this application lead to the identification of several platform specific factors that influence eye feature detection and accuracy. Here, we mention few of the factors that have significant influence on the detection of eye features: Eyebrows [11, 17, 18, 36]; Eyelids [34]; Hair [47]; Head rotation and Pose [35, 44, 63]; Imaging condition and quality [4,9,11,35,41,44,47,51,54]; Semiclosed eyes [7,26,35,48,49]; Spectacles [5,7,8,11,17,22,26,29,30,32,34,36,47–51,53,55,58,60,63]; Squinted eyes [13]; Wrinkles, dark circles, swells, and cosmetics [54,56].

Of the challenges mentioned above, two standout the most: Spectacles and illumination. [1,4,13,34,41,54,59] circumambulate these challenges by working on facial images without spectacles only. Among [5,7,8,48,49,55,60,63] - which dealt with spectacle images, papers related to eye corner detection are [49,55] only. We term the challenges that arise from the usage of spectacles as the spectacle problem [22].

2 Spectacle problem

Though spectacles occupy fewer area in-terms of number of pixels, it has a huge impact on face feature detection as well as tracking algorithms. Two problems occur when the user wears spectacles (see Fig.1). They are:

- Occlusion: Occlusion is the phenomena in which eye features are obstructed by the spectacle frame. Depending upon the comfort, nature, and size of spectacle frame used - most or partial amount of eye feature information may be lost [5, 6, 12, 17, 22, 29].
- Illumination changes: Glare and secondary reflections occur due to the variation in illumination projected on to the human subjects. These variations result in an apparent change on the reflectance properties of the spectacles leading to a visual variation of the eye features [12, 17, 22, 32, 36, 58].

All the spectacle problem elements individually or cumulatively can vary or obstruct the appearance of the eye features. These factors pose great challenges to the existing eye corner detection strategies. However, little research has been done addressing these issues [11]. One of the major reason being that most of the

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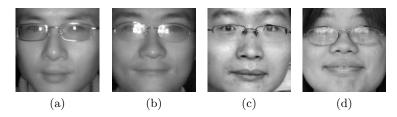


Fig. 1: Sample images from CASIA NIR-VIS 2.0 database [27] illustrating the Spectacle problem. (a),(b) Glare; (c) Occlusion; (d) Secondary reflection

available databases have been collected under well controlled laboratory conditions with normal lighting, neutral expression and high image quality [44]. Such conditions generally do not represent the real-time challenges like the spectacle problems.

3 Datasets

TABLE 1 provides a brief overview of the most used databases in the research field of eye feature detection. This review helps the researchers to choose an appropriate database for their specific research.

Name of the database	Variation in				
	Illumination	Pose	Expression	Accessories	Session
MIT database [2]					
ORL database [39]	\checkmark	\checkmark	\checkmark	\checkmark	
AR face database [31]					
CurtinFaces dataset [25]					
FEI face database [46]					
COFW [5]		\checkmark	\checkmark	\checkmark	
300 faces in-the-wild [38]					
XM2VTSDB [33]				\checkmark	\checkmark
KFDB [15]	\checkmark	\checkmark	\checkmark	\checkmark	
LWIR imagery [42]	\checkmark		\checkmark	\checkmark	
CASIA NIR-VIS 2.0 database [27]					\checkmark
YALE database [3]	\checkmark		\checkmark	\checkmark	
CASIAWebFace [57]				\checkmark	
LFW [14]	\checkmark	\checkmark	\checkmark	\checkmark	
CAS-PEAL [12]	\checkmark	\checkmark	\checkmark	\checkmark	
FERET database [37]	\checkmark	\checkmark		\checkmark	\checkmark
Indian database [23]	\checkmark	\checkmark	\checkmark	\checkmark	\checkmark

Table 1: Real-life scenario databases and their variabilities considered.

3.1 Summary of database review

- Illumination: [42] provides thermal facial imagery, whereas [27] provides facial images captured in NIR illumination. NIR and thermal imaging conditions do not mimic real-time visible conditions. [2, 25, 31, 46, 57] databases are created in visible illumination conditions, but the variation levels are limited. Among the remaining databases, [23, 37] images are captured at low, medium and high illumination conditions of an office environment.
- Accessories (here spectacles): Structural differences in glasses can change the appearance of an individual. Spectacles used in [12] have almost identical shapes, sizes and colors. Therefore, the variation that the accessories bring is not prominent. [23] database have considered the usage of various spectacle frames: Full-rim, Half-rim, and Rim-less - resulting in a larger accessory variation.
- Ground-truth: Most of the available databases focus on face detection and recognition. So, the ground-truth information of the eye feature information is hardly found [43]. Also in case of spectacle problem removal algorithms, we need to have pairs of corresponding face images with and without eyeglasses for verifying the seamlessness of the spectacle removal algorithm outputs. Such ground-truth images along with spectacle problem free image and eye corner location details is provided in [23, 29, 51].
- Database size: Using private large-scale training datasets, several samplebased algorithms achieve huge success in terms of adaptability and performance. While there are many open source implementations of the algorithms, none of the large-scale face dataset with spectacles is publicly available. [37] considered many variation factors but the quantity of images is very less when compared to [23].

4 Spectacle problem removal: Previous approaches

Due to the unpredictability caused by occlusion, glare and secondary reflection formations, the spectacle removal problem is quite challenging than the detection application [44]. Depending upon the number of input images used to rectify the spectacle problem, the methods can be classified as: Single image based and Multiple image based approaches.

5 Single image approach

One of the most commonly used single image based approach is the image inpainting based approach [28, 45]. Image inpainting techniques are more suitable for texture synthesis applications only and tend to fail in generating a seamless output image in case of facial images [58]. [40] proposed an anti-glare algorithm, in which they assumed that the reflection occurs proportionately on both the eyes. In real-time scenarios, this reflection assumption does not hold good and therefore limits the usability of the algorithm to synthetic images only. In [24] 6 M.Z.Lazarus et al.

approach, a user has to physically mark the regions in which there are traces of reflection. This approach is more efficient in terms of output results but, the effort and precision of the user will influence the algorithm. [17] proposed a phase congruency based approach, but the algorithms efficiency degrades when the user wear a full-rim spectacle-frame (see Fig. 2).

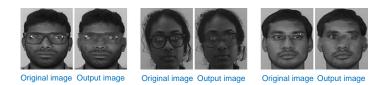


Fig. 2: Sample output images of single image based approach [17].

5.1 Multiple image approaches

[36, 51] are sample-based approaches that learn from the statistical mapping between face images with and without spectacles to generate a seamless facial image without spectacle problem. The problem with these approaches is that the representational power of these algorithms depends on the training set. [28] adopts a new hybrid approach by combining inpainting and deep learning technique for spectacle problem removal. A more generalized de-occlusion algorithm is reported in [61]. [22] is based on the assumption that facial images subjected to various illumination conditions tend to lie on a low-dimensional Lambertian space. Therefore, a given sequence of multiple images is decomposed into the Low rank and Sparse component. The low-rank layer retains most of the uncorrupted facial features while the sparse layer retains the pixels related to the spectacle problem. Even though the multiple image based approaches perform much better than the single image based approaches, one might experience the following limitations.

Limitations

- Performance of multiple based approaches depend on the facial image alignment. This is a unrealistic assumption as in real-time scenarios, the subject might continuously change his/her head position. Large head movements can cause some time-aliasing artifacts to appear in the output image.
- Because of the usage of a large number of input images: resource, computational, and time complexity of these multiple image based methods is quite large.
- The output images fail to extract the eye image dynamics (see Fig. 3). This would be a serious problem in case of eye tracking applications.

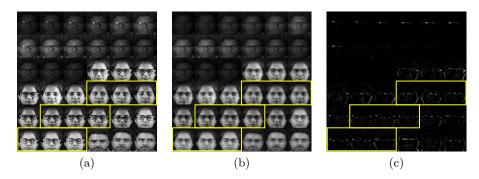


Fig. 3: Result of [22]. Each sub-plot contains (a) original, (b) reconstructed and (c) error component images respectively. The ineffectiveness of recovering the eye feature dynamics is highlighted in yellow.

6 Experimentation

In this section, we conduct a landmark localization experiments to highlight the impact of spectacle problem. We have considered CNN based algorithm presented in [20], for determining the influence of illumination level and spectacles on the detection accuracy of facial landmark localization. We have created a ground-truth of manually generated facial landmarks for a subset of 1,600 images from [23] database. For a test-bench containing facial images without spectacles, the images subjected to high illumination level have least average localization error values as compared to the poorly illuminated images (Fig. 4(a)). This showcases the influence of illumination on landmark localization. Similar experiment on a test-bench of images subjected to the same illumination levels reveals that the localization error rate increases for images with spectacle problem (Fig. 4(b)).

Due to the error in landmark localization, application related to humancomputer-interaction systems also suffer. In Fig. 5 we present the influence of inaccurate eye feature localization on eye-blink detection as an example.



Fig. 5: Sample images highlighting the influence of spectacles on eye localization.

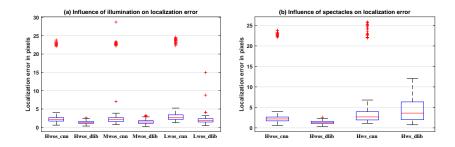


Fig. 4: Error distribution highlighting the influence of (a) illumination and (b) spectacles on the localization of face features. Where H: High, M: Medium, L: Low illumination level; wos: Without spectacles, ws: with spectacles; dlib and cnn methods as proposed in [20].

7 Conclusion

Accurate eye feature detection, localization and tracking is a preliminary but important step in the spectrum of disciplines like human-computer-interaction, biometrics, alertness-level detection applications. In this article, we attempt to present a comprehensive survey on the state-of-the-art eye corner detection techniques. The review focuses on real-life scenarios wherein the subject wear spectacles and the research challenges that comes along with it. Recent developments in the topic related to spectacle problem removal approaches is also presented and discussed. Due to the inherent complexity of the spectacle problem and its wide practical applications in science, society, research and industry, we believe that this area will draw increasing attention from a variety of fields beyond image processing and machine learning.

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